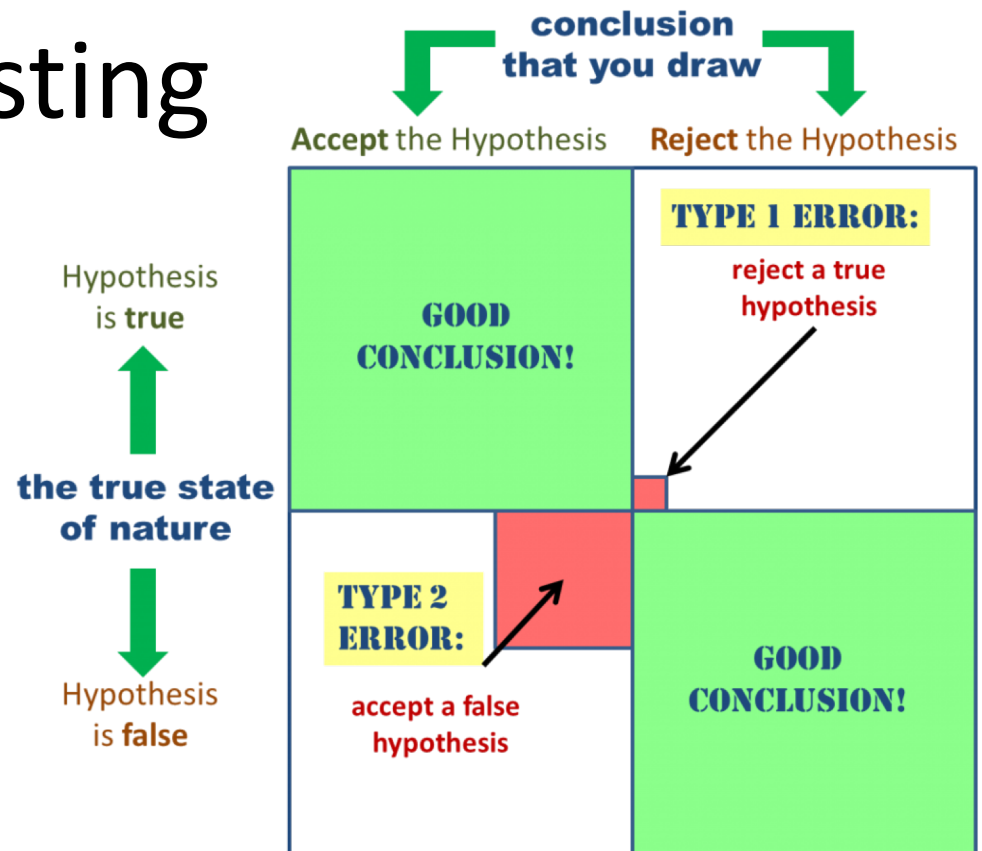


Hypothesis Testing



A man walks into a bar...

- You are sitting in a bar and the man next to you says "I'll flip a coin. If it comes up heads, buy me a drink. If it comes up tails, I will buy you a drink."
- You agree...



The outcome

- H
 - HH
 - HHH
 - HHHH
 - HHHHH
 - HHHHHH
 - HHHHHHH
 - HHHHHHHH
- $P(H) = \frac{1}{2}$
 - $P(HH) = \frac{1}{2} \times \frac{1}{2} = 0.25$
 - $P(HHH) = (\frac{1}{2})^3 = 0.125$
 - $P(HHHH) = (\frac{1}{2})^4 = 0.063$
 - $P(HHHHH) = (\frac{1}{2})^5 = 0.031$ $p < .05$
 - $P(HHHHHH) = (\frac{1}{2})^6 = 0.016$
 - $P(HHHHHHH) = (\frac{1}{2})^7 = 0.008$ $p < .01$
 - $P(HHHHHHHH) = (\frac{1}{2})^8 = 0.004$

Are you being cheated?

A statistician's approach

- **Null hypothesis** – $H_0: p(H) = \frac{1}{2}$
the coin is fair (no cheating)
- **Alternative hypothesis** – $H_1: p(H) \neq \frac{1}{2}$
the coin is not fair (cheating)
- **Hypothesis test** - if $P(\text{event}) < .05$ reject null hypothesis

Note: null hypothesis is needed to calculate probabilities

Short list of steps in Hypothesis testing

1. State your research question
2. Specify the null and alternative hypotheses (H_0 versus H_a)
3. Implement the appropriate test
4. Evaluate output and make decision: “reject” or “fail to reject” the null hypothesis based on p-value
5. Interpret the results in context

Interpreting a P -value

Could random variation alone account for the difference between the null hypothesis and observations from a sample?

- A small P -value (<0.05) implies that random variation (due to the sampling process alone) is not likely to account for the observed difference.
- With a small P -value ($p < 0.05$), we **reject H_0** . The true mean or proportion of the population is **significantly** different from what was stated in H_0 .

Thus small P -values are strong evidence AGAINST H_0 .

Determine the appropriate test

Response Explanatory		
	categorical	quantitative
categorical	C → C	C → Q
quantitative	Q → C	Q → Q

ChiSQ

ANOVA

Explanatory=Independent Variable
Response=Dependent Variable

r correlation

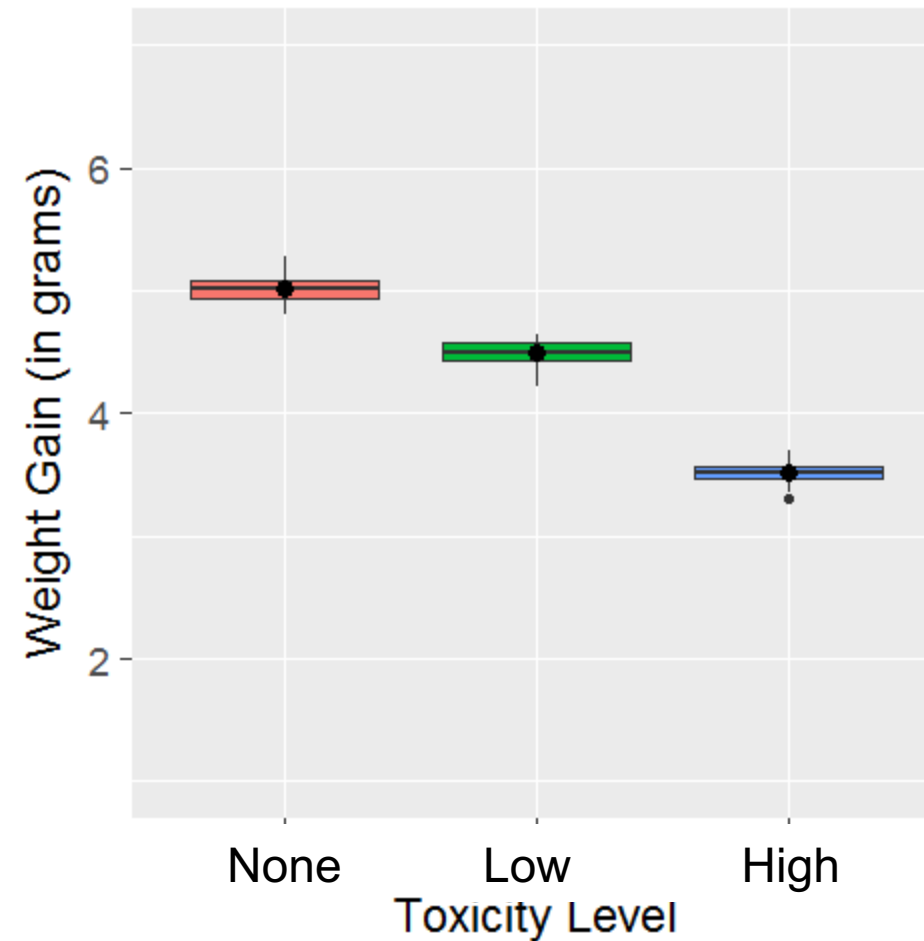
Analysis of Variance

ANOVA

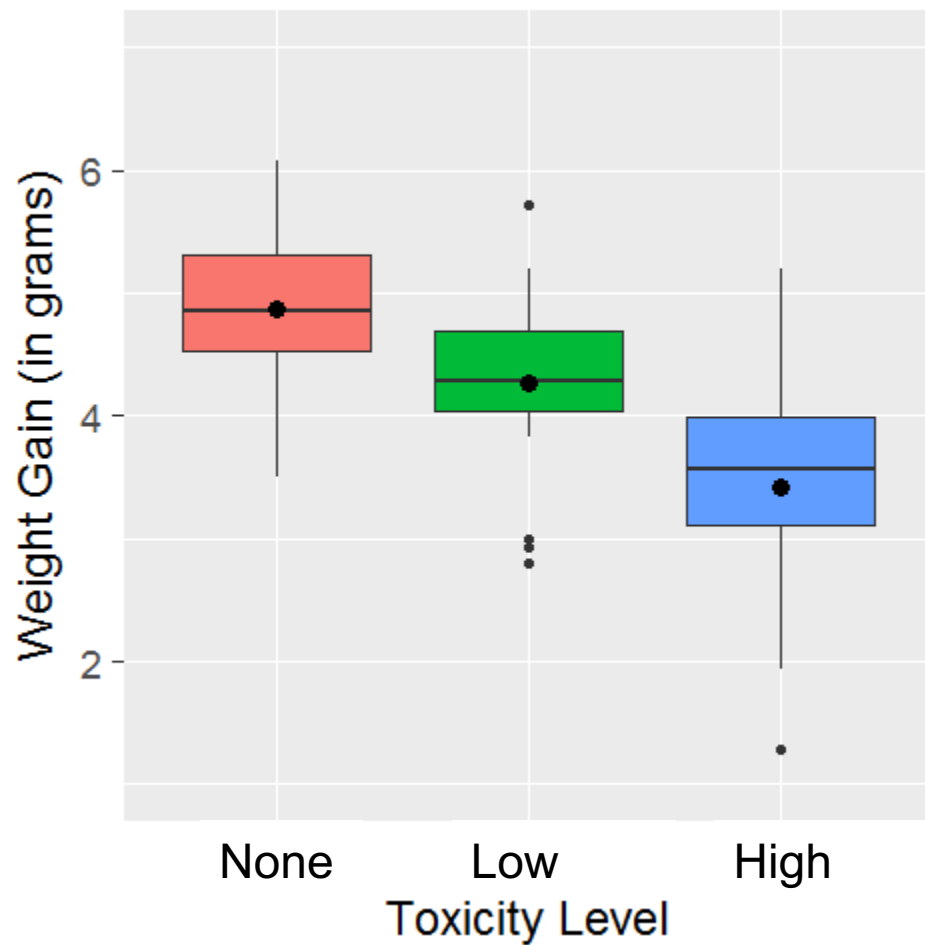
ANOVA

$C \rightarrow Q$ (comparing means, Q – DV, among two or more categories, C – IV)

Scenario 1



Scenario 2



F = Variability Between Groups / Variability within Groups

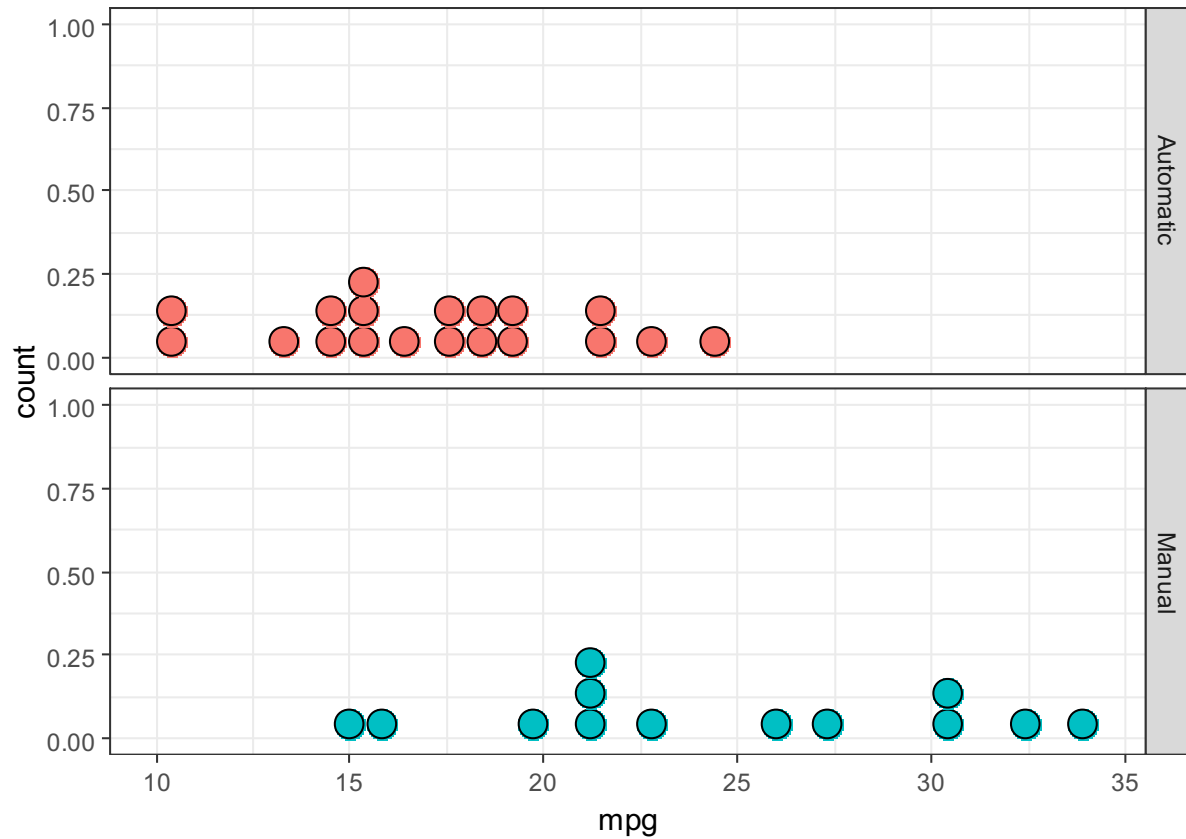
Scenario 1

Source	Df	SS	MS	F	P-value
Toxicity	2	26.83	13.41	67.05	<0.001
Residuals	57	11.41	0.200		

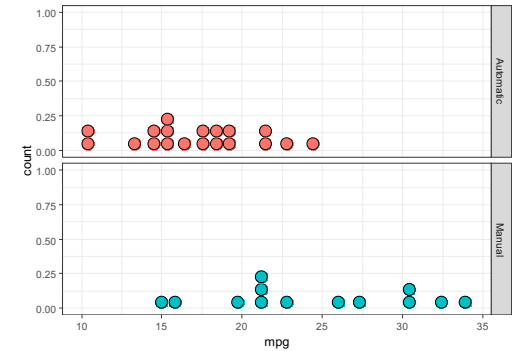
Scenario 2

Source	Df	SS	MS	F	P-value
Toxicity	2	27.37	13.69	11.8	<0.001
Residuals	57	66.07	1.16		

MPG vs. Transmission Type

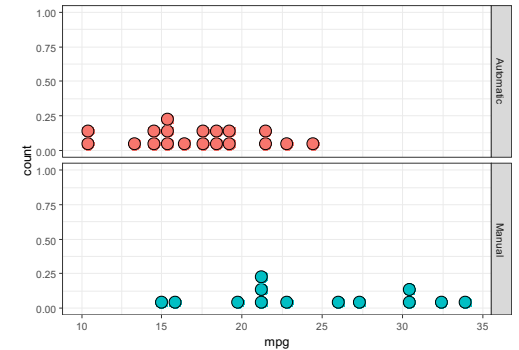


ANOVA Table



	Df	Sum Sq	Mean Sq	F value	Pr(>F)
transmission	1	405.2	405.2	16.86	0.000285
Residuals	30	720.9	24.0		

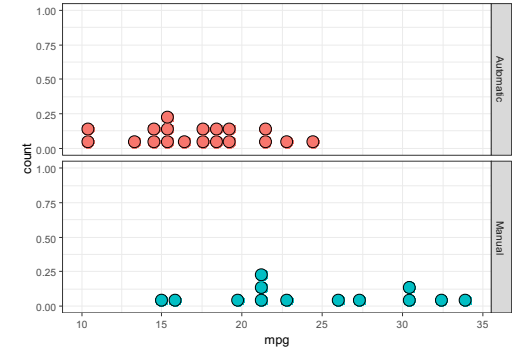
ANOVA Table



	Df	Sum Sq	Mean Sq	F value	Pr(>F)
transmission	1	405.2	405.2	16.86	0.000285
Residuals	30	720.9	24.0		

F = variability between groups/variability within groups

ANOVA Table

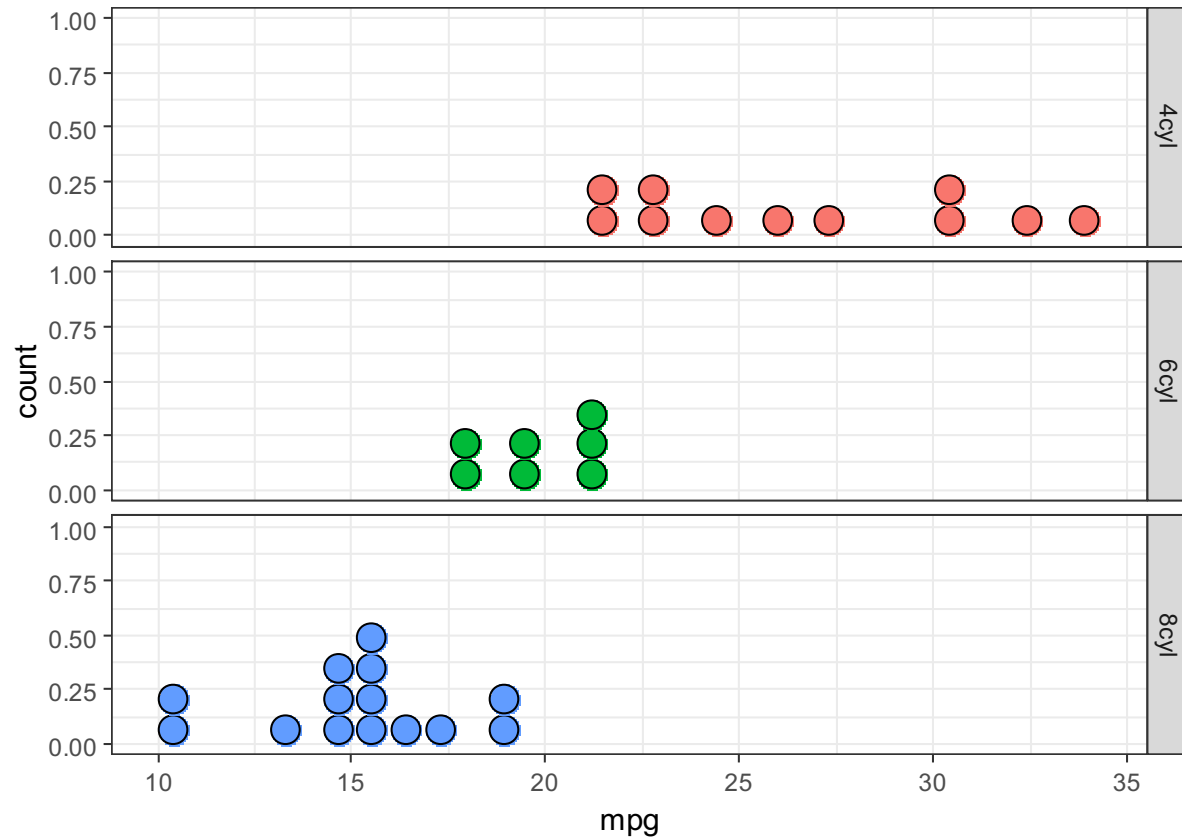


	Df	Sum Sq	Mean Sq	F value	Pr(>F)
transmission	1	405.2	405.2	16.86	0.000285
Residuals	30	720.9	24.0		

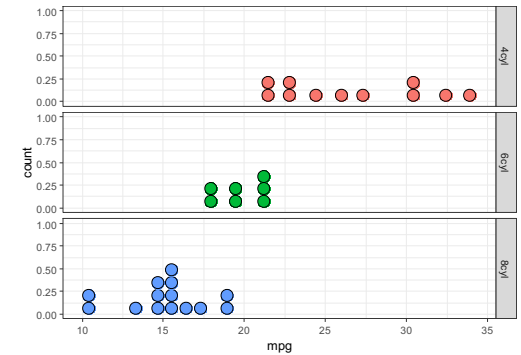


Probability of obtaining an F value this large or larger given H_0 is true.

MPG vs. Cylinder

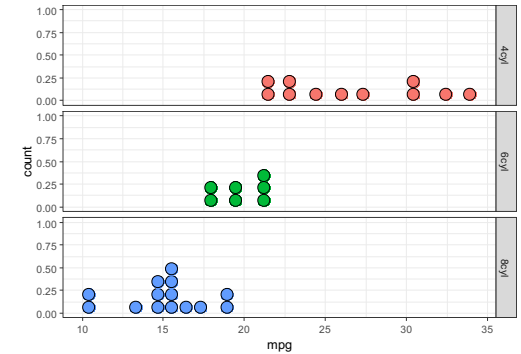


ANOVA Table



	Df	Sum Sq	Mean Sq	F value	Pr(>F)
cyl	2	824.8	412.4	39.7	4.98e-09
Residuals	29	301.3	10.4		

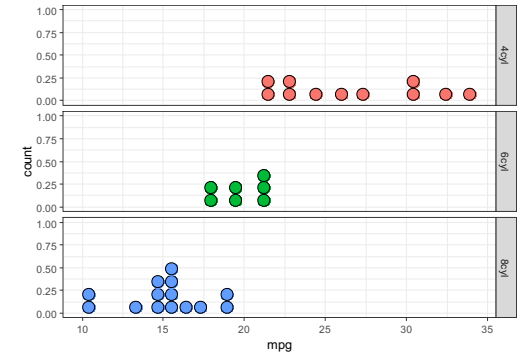
ANOVA Table



	Df	Sum Sq	Mean Sq	F value	Pr(>F)
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ANOVA Table



	Df	Sum Sq	Mean Sq	F value	Pr(>F)
cyl	2	824.8	412.4	39.7	4.98e-09
Residuals	29	301.3	10.4		



Probability of obtaining an F value this large or larger given H_0 is true.

Post Hoc Comparisons

		diff	lwr	upr	p adj
6cyl-4cyl	-6.920779	-10.769350	-3.0722086	0.0003424	
8cyl-4cyl	-11.563636	-14.770779	-8.3564942	0.0000000	
8cyl-6cyl	-4.642857	-8.327583	-0.9581313	0.0112287	

Comparison of mpg by cyl
(Sidak)

Row Mean- Col Mean	4	6
6	-6.92078 0.000	
8	-11.5636 0.000	-4.64286 0.012